# **Nonslender Waveriders**

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A new body-oriented procedure for generating nonslender waverider shapes is described. These shapes are more practical than conventional waveriders that are relatively slender. Aside from slenderness, the method provides control over the included angle at the leading edge of the waverider, which is structurally important. A new procedure for rounding the leading edge is also presented. Although the lift-to-drag ratio is less for a nonslender waverider, relative to a slender one, it is still quite large. Lift-to-drag is thus traded for improved volumetric effectiveness, thicker winglets, and easier matching with the aft portion of a waverider-based vehicle. By means of hypersonic small-disturbance theory, an on-design parametric study is performed. Off-design performance is provided by solutions of an Euler space-marching code. Both studies verify the feasibility for developing nonslender waveriders.

#### **Nomenclature**

A, B = coefficients for freestream curve  $A_h$  = waverider base plane area

 $b^{*}$  = width of waverider in the base plane

 $C_D$  = drag coefficient

 $C_{D \text{ inv}}$  = inviscid drag coefficient

 $C_f$  = average skin friction coefficient

 $\vec{C_L}$  = lift coefficient

 $K_{\delta}$  = hypersonic similarity parameter,  $M_{\infty}\delta$ 

L/D = lift-to-drag ratio l = length of basic cone  $l_w$  = length of waverider  $M_\infty$  = freestream Mach number  $M_\infty$  = design Mach number

 $R_0$  = normalized radial distance to freestream surface

in symmetry plane

 $S_b$  = shock layer base plane area  $S_p$  = projected planform area  $S_w$  = wetted surface area

t = waverider thickness in the base and symmetry

planes

V = volume of waverider

X, Y = normalized Cartesian coordinates in the base

plane

 $X_{\sigma}$ ,  $Y_{\sigma}$  = normalized shock location in the base

plane

 $\alpha$  = angle of attack  $\beta$  = shock angle

 $\gamma$  = ratio of specific heats  $\delta$  = half cone angle

 $\delta$  = half cone angle  $\eta$  = volumetric parameter,  $V^{2/3}/S$ 

 $\Lambda_b$  = waverider edge angle in the base plane  $\Lambda_{be}$  = maximum waverider edge angle in the base

plane

 $\Lambda_n = \text{waverider edge angle at nose}$ = ratio of shock angle to cone angle

 $\tau$  = thickness ratio  $\phi_t$  = anhedral angle

 $\hat{\Omega}_{\infty}$  = slope angle of freestream surface at edge in the base plane

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## Introduction

AVERIDER-BASED vehicles are of interest for supersonic and hypersonic flight since they provide a large L/D. In 1990, the First International Hypersonic Waverider Symposium was devoted to this technology. Since the symposium, additional publications have appeared. 1-5 A common element of the analysis in these publications is that waveriders are typically viewed as slender vehicles. This has led to difficulties when attempting to mate a waverider forebody with the rest of the vehicle. The aft portion would prefer a thicker forebody, particularly in the base plane of the waverider where they merge. A nonslender waverider would provide better packaging, and a reduction in the skin friction of the forebody. A slender waverider generally possesses a sharp leading edge, which is not realistic, and a thin structure adjacent to the leading edge. This leading edge may not be able to handle the large structural and heat transfer loads. These are important limitations blocking future development of waveriders.

Hypersonic small-disturbance theory (HSDT) is used to establish a new approach for the design of nonslender waveriders. As expected, the wave drag is increased relative to a slender waverider counterpart, and the L/D is less. However, one can show that a high L/D forebody does not imply a large L/D for the integrated vehicle. The overall reduction in L/D is partly offset because the nonslender waverider has less viscous drag compared to that of a slender waverider. The design approach presented here controls the magnitude of the included angle between the freestream and compression surfaces at the leading edge. Along with rounding, this feature overcomes the problems associated with a thin structure near the leading edge.

The object of this work is to develop a generic design approach that yields practical waverider configurations. In this context, we assume an endoatmospheric vehicle and choose its design point to coincide with its maximum anticipated hypersonic flight Mach number,  $M_{\infty d}$ . At this condition, the vehicle experiences its maximum drag and heat transfer. A major benefit of this approach is that the bow shock is detached when  $M_{\infty} < M_{\infty d}$ . This is in contrast to the interaction, downstream of the leading edge, between the shock wave and boundary layer that occurs when  $M_{\infty} > M_{\infty d}$ . This interaction can result in boundary-layer separation and a large local heat transfer rate. Other benefits are discussed later. Therefore, when off-design performance is evaluated,  $M_{\infty}$  will not exceed the  $M_{\infty d}$  design value.

In the next section, the HSDT approach is developed. We also describe the Euler code used to validate the HSDT and to perform off-design calculations. This section concludes with a brief discussion of leading-edge rounding. The next section provides on- and off-design results for geometric and aero-dynamic waverider properties. The final section contains a summary of our findings. The dissertation by He<sup>6</sup> should be consulted for additional details that cannot be included here.

#### **Formulation**

#### Hypersonic Small-Disturbance Theory

Inviscid, supersonic flow of a perfect gas is considered about a cone at zero incidence. The coordinate system and much of the nomenclature is shown in Fig. 1. Aside from  $\gamma$  (=1.4), the conical flowfield between the shock and cone is governed by  $\delta$  and  $M_{\infty}$ . With the aid of HSDT, <sup>6-8</sup> the shock wave angle is given by

$$\sigma \equiv \frac{\beta}{\delta} = \left[ \frac{\gamma + 1}{2} + \frac{1}{K_{\delta}^2} \right]^{1/2} \tag{1}$$

where  $K_{\delta} = M_{\infty}\delta$ . Following Refs. 7 and 8, it is convenient to consider waveriders that have a freestream curve in the base plane determined by an even polynomial

$$X = R_0 + AY^2 + BY^4 \tag{2}$$

where X, Y, and  $R_0$  are normalized using  $l\delta$  (Fig. 1). The A and B coefficients are usually found by specifying  $R_0$  and  $\phi_t$ , which are coordinate dependent. A different system of body-oriented parameters, however, will be introduced to expedite the design of nonslender waveriders. A higher degree polynomial, as well as other forms, can be used for Eq. (2). The basic approach is not dependent on the specific representation of the freestream curve.

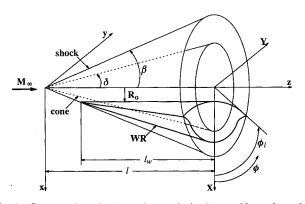


Fig. 1 Construction of a general cone-derived waverider, where the  $X,\ Y$  coordinates are shown in the base plane.

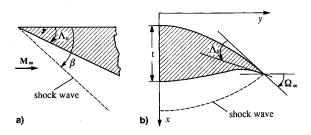


Fig. 2 Schematic showing a) nose angle  $\Lambda_n$  in the symmetry plane and b) t and  $\Lambda_b$  and  $\Omega_\infty$  in the base plane.

Figure 2 shows the freestream surface angle at the edge in the base plane  $(\Omega_{\infty})$ . This specified parameter is related to A and B through

$$\tan \Omega_{\infty} = \left(\frac{\mathrm{d}X_{\infty}}{\mathrm{d}Y_{\infty}}\right)_{\sigma} = \left(2AY_{\infty} + 4BY_{\infty}^{3}\right)_{\sigma}$$

where the  $\sigma$  subscript denotes the leading edge in the base plane, and

$$X_{\sigma} = \sigma \cos \phi_l, \qquad Y_{\sigma} = \sigma \sin \phi_l$$
 (3)

We thus obtain

$$A + 2(\sigma \sin \phi_l)^2 B = \frac{\tan \Omega_{\infty}}{2\sigma \sin \phi_l}$$
 (4)

Equations (2) and (3) also yield the leading-edge constraint

$$A + (\sigma \sin \phi_l)^2 B = \frac{\sigma \cos \phi_l - R_0}{(\sigma \sin \phi_l)^2}$$
 (5)

Figure 2 also shows the edge angle  $\Lambda$  whose exact value at the nose is<sup>8</sup>

$$\Lambda_n = \beta - \tan^{-1} \left[ \frac{2 + (\gamma - 1)M_{\infty}^2 \sin \beta^2}{(\gamma + 1)M_{\infty}^2 \sin \beta \cos \beta} \right]$$

When  $\beta$  is small, the HSDT form is

$$M_{\infty}\Lambda_n \triangleq \frac{K_{\delta}^2}{[1+(\gamma+1)K_{\delta}^2/2]^{1/2}} = \frac{K_{\delta}}{\sigma}$$

Thus,  $M_{\infty}\Lambda_n$  is determined by  $K_{\delta}$ , and does not depend on any of the parameters that define the shape of the waverider. Figure 3 shows  $(M_{\infty}\Lambda_n)/10$  with  $\Lambda_n$  in degrees. (All angles in the figures and table are in degrees.) For a waverider with  $M_{\infty d}=8$  and  $\delta=10$  deg,  $\Lambda_n$  equals 7.5 deg. While this is not a large angle,  $\Lambda_n$  would be only 3.7 deg if  $\delta=6$  deg, a frequently encountered value for  $\delta$ . Thus, a relatively large value for  $\delta$  is required for a useful  $\Lambda_n$  value.

By definition, the included edge angle  $\Lambda$  is in a plane normal to the leading edge. The leading edge in the base plane,

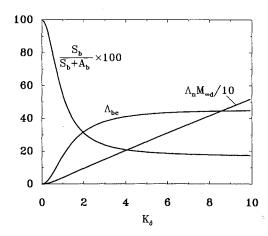


Fig. 3 Angles  $(\Lambda_n M_{\infty d})/10$  and  $\Lambda_{be}$ , and the shock layer fractional area as a function of the hypersonic similarity parameter.

however, typically has a sweep angle in excess of 70 deg; we therefore approximately evaluate  $\Lambda_b$  in the base plane as<sup>6</sup>

$$\tan \Lambda_b = \frac{\sin(\Omega_x + \phi_l)\cos(\Omega_x + \phi_l)}{\sigma^2 - \sin^2(\Omega_x + \phi_l)}$$
 (6)

With  $\sigma$  fixed,  $\Lambda_b$  has a maximum value determined by  $\partial \Lambda_b / \partial \Omega_{\infty} = 0$ , or  $\partial \Lambda_b / \partial \phi_l = 0$ . This yields

$$\Lambda_{be} = \sin^{-1}\left(\frac{1}{2\sigma^2 - 1}\right) = \sin^{-1}\left(\frac{K_\delta^2}{2 + \gamma K_\delta^2}\right)$$

where the e subscript denotes an extremum, and  $\Lambda_{be}$  is shown in Fig. 3. For  $M_{\infty d}=8$  and  $\delta=10$  deg,  $\sigma$  is 1.309 and  $\Lambda_{be}=24.3$  deg; hence, the base plane edge angle can be substantial. As with  $\Lambda_n$ , this is true only if  $\delta$  is not too small. For instance, if  $\delta=6$  deg, then  $\Lambda_{be}$  is only 13.6 deg. The actual edge angle is given by

$$\Lambda_h = \Lambda_n + \omega_{\Lambda}(\Lambda_{he} - \Lambda_n)$$

and only depends on  $\delta$ ,  $M_{\times d}$ , and  $\omega_{\Lambda}$ , where  $\omega_{\Lambda}$  is specified and ranges from 0 to 1. Thus, when  $\omega_{\Lambda} > 0$ ,  $\Lambda$  varies smoothly from its minimum  $\Lambda_n$  value at the nose to its maximum value in the base plane.

With  $\sigma$ ,  $\dot{\Lambda}_b$ , and  $\Omega_{\infty}$  known, Eq. (6) provides  $\phi_l$ , which is required later. By inverting this equation, we obtain

$$\phi_t = -\Omega_{\infty} + \tan^{-1} \left[ \frac{1 - \sqrt{1 - 4\sigma^2(\sigma^2 - 1)\tan^2\Lambda_b}}{2(\sigma^2 - 1)\tan\Lambda_b} \right]$$

The value for  $\Omega_{\infty}$  is not entirely arbitrary; we constrain it by requiring that  $0 \le \phi_l \le \pi/2$ . This results in

$$\Omega_{\infty, \min} \leq \Omega_{\infty} \leq \Omega_{\infty, \max}$$

where

$$\Omega_{\infty, \max} = \tan^{-1} \left[ \frac{1 - \sqrt{1 - 4\sigma^2(\sigma^2 - 1)\tan^2 \Lambda_b}}{2(\sigma^2 - 1)\tan \Lambda_b} \right]$$

$$\Omega_{\infty, \min} = \Omega_{\infty, \max} - \frac{\pi}{2}$$

For  $M_{\infty d}=8$  and  $\delta=10$  deg,  $\Omega_{\infty, \min}$  and  $\Omega_{\infty, \max}$  are -33.3 and 56.7 deg, respectively. It is useful to note that these bounds depend only on  $\delta$ ,  $M_{\infty d}$ , and  $\omega_{\Lambda}$ .

The thickness t (Fig. 2b) can be written nondimensionally as

$$\tau = \frac{t}{\delta l_w} = \frac{\left[1 + (\sigma^2 - 1)R_0^2/\sigma^2\right]^{1/2} - R_0}{1 - (R_0/\sigma)}$$
(8a)

where  $R_0$  and  $l_w$  are shown in Fig. 1. The parameter  $\tau$ , referred to as the thickness ratio, represents the normalized thickness of the waverider in the symmetry and base planes. Inversion of Eq. (8a) yields

$$R_0 = \sigma \frac{1 - \tau^2}{2\sigma\tau - (1 + \tau^2)}$$
 (8b)

As with  $\phi_l$  and  $\Omega_{\infty}$ , there are practical limits on  $R_0$  and  $\tau$ . The first  $R_0$  constraint stems from the requirement that the compression surface not cross over the freestream surface. This requirement is equivalent to

$$\frac{\mathrm{d}}{\mathrm{d}Y} \left( \frac{Y}{X} \right) \ge 0, \qquad 0 < Y < Y_{\sigma}$$

or

$$R_0 - AY^2 - 3BY^4 \ge 0, \quad 0 < Y < Y_a$$

where A and B are given by Eqs. (4) and (5). The equality sign yields a minimum value for  $R_0$ , i.e.

$$R_{0,\min} = (\sigma/8)\cos\phi_l \{5 - 2 \tan\phi_l \tan\Omega_{\infty} - [3(3 - \tan\phi_l \tan\Omega_{\infty})(1 - \tan\phi_l \tan\Omega_{\infty})]^{1/2}\}$$

where  $\phi_l$  is given by Eq. (7). For  $R_{0,\text{max}}$ , we arbitrarily set

$$R_{0,\text{max}} = X_{\sigma} = \sigma \cos \phi_{l}$$

which corresponds to a waverider with a planar upper surface when  $\Omega_{\infty} = 0$ . With Eq. (8a), this yields

$$\tau_{\min} = \frac{-R_{0,\max}\sigma + \sqrt{R_{0,\max}^2\sigma^2 + (\sigma^2 - R_{0,\max}^2)}}{\sigma - R_{0,\max}}$$

$$\tau_{\max} = \frac{-R_{0,\min}\sigma + \sqrt{R_{0,\min}^2 \sigma^2 + (\sigma^2 - R_{0,\min}^2)}}{\sigma - R_{0,\min}}$$

where

$$0 < \tau_{\min} \le \tau \le \tau_{\max} < 1$$

In parallel with  $\Lambda_b$ ,  $\tau$  is determined by

$$\tau = \tau_{\min} + \omega_{\tau}(\tau_{\max} - \tau_{\min})$$

where  $\omega_{\tau}$  ranges from 0 to 1. The parameter  $\omega_{\tau}$  controls the shape of the waverider in the base plane, for given values of  $\Omega_{\infty}$  and  $\omega_{\Lambda}$ . When  $\omega_{\tau}=0$  and  $\Omega_{\infty}=0$ , the configuration is slender with a planar upper surface. When  $\omega_{\tau}=1$ , it is less slender, but the freestream and compression surfaces touch for a Y where  $0 < Y < Y_{\sigma}$ .

The foregoing procedure determines the waverider configuration once  $\delta$ ,  $M_{\infty d}$ ,  $\Omega_{\infty}$ ,  $\omega_{\Lambda}$ , and  $\omega_{\tau}$  are specified. These include its overall dimensions, i.e., length  $(l_{w}/l)$ , span (b/l), and thickness (t/l), the latter two are in the base plane. The parameters  $\sigma$ ,  $R_0$ ,  $\phi_l$ , A, B, . . . are still useful, since they appear in the elegant quadrature procedure 7.8 that determines geometric properties such as  $S_w$  and V, and aerodynamic properties such as the lift and drag. Equations (1), (4), (5), (7), and (8b) are utilized for determining geometric properties.

One important parameter, not previously obtained, is the ratio of the shock layer area,  $S_b$ , to the total area (between the freestream and shock curves) in the base plane. This ratio is

$$\frac{S_b}{S_b + A_b} = \frac{\sigma^2 - 1}{\sigma^2} = \frac{1 + (\gamma - 1)K_b^2/2}{1 + (\gamma + 1)K_b^2/2}$$

and is shown in Fig. 3. Thus, the maximum shock layer area in the base plane that is available for a scramjet inlet is a fixed fraction of the total base area and is independent of the waverider shape. For the earlier case  $(M_{\infty d} = 8 \text{ and } \delta = 10 \text{ deg})$ , this fraction is 0.416.

# **Euler Algorithm**

The Lawrence PNS space marching code<sup>9</sup> is used in its Euler version. Since the waverider shape is nonconical, an initial-data plane is supplied at a distance of 1% of  $l_w$ , measured from the nose. The initial data can come from HSDT, for ondesign operation, or a time-marching Euler code for both onand off-design operation. The space-marching code is used because of its computational efficiency. A detailed comparison of solutions in the base plane verified the accuracy of

this approach.<sup>6</sup> The grid generation technique used was developed by Thompson.<sup>10</sup> Grid lines are obtained by solving Poisson's equation with source terms as control functions. The grid for an inviscid calculation of a sharp-edged waverider with the space-marching code is  $64 \times 41$  and  $67 \times 41$  for a rounded leading edge.

#### Leading-Edge Rounding

The first investigation<sup>11</sup> of edge rounding experimentally showed that the pressure is affected only close to the leading edge. More recently, Refs. 2 and 4 have computationally reexamined this topic. In particular, Ref. 4 used a circular arc to round the edge whose radius appreciably increased with downstream distance. As in Ref. 11, pressure changes occur only close to the leading edge, a result our calculations reconfirm. More importantly, Vanmol and Anderson<sup>4</sup> point out that the nature of the boundary layer on the freestream and compression surfaces is affected by rounding, particulary by the induced crossflow velocity. Thus, rounding can have an important effect on both skin friction and heat transfer.

Since we desire a smooth, as well as flexible, curve to replace the sharp edge, a third-order continuous B-spline curve is used.<sup>6</sup> As a consequence, the surface has both continuous first derivatives and continuous curvatures. (A discontinuous curvature in a supersonic flow may lead to boundary-layer separation.) In order that the variation of the radius of curvature normal to the edge be approximately uniform, the rounding near the nose is about 3% of the local span, while

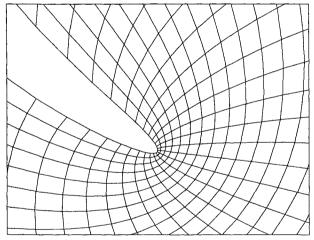


Fig. 4 Computational grid near a rounded leading edge.

only 1% of the span in the base plane. A highly expanded view of the grid at a rounded edge is shown in Fig. 4.

#### Results

We consider waverider forebodies with a 20-m length that are flying at a 24-km altitude. The corresponding Reynolds number,  $(\rho V l_w/\mu)_{\infty}$ , is  $1.55 \times 10^8$ . On-design results, based on HSDT, are first presented.

#### **On-Design Results**

Table 1 summarizes the parametric analysis, where the first five rows are input, the next six rows show geometric output, while the last six rows contain lift and drag values. Laminar results in this last group are based on the theory in Ref. 8, and are meant to provide trends. (Nevertheless, the boundary layer on a free-flight 10-deg cone at  $M_{\infty} = 3$  was still laminar at the largest Reynolds number,  $5 \times 10^7$ , of the experiment. <sup>12</sup>)

Configuration 1 in Table 1 is a nominal case; several views of it are shown in Fig. 5. This configuration is not an optimum one, either in terms of  $\eta$  or L/D. Other configurations, i.e., number 4, have larger  $\eta$  and L/D values. Configuration 1, however, is typical of the nonslender shapes generated with this approach. Noteworthy points are the sizable edge angle  $\Lambda_b$  (= 24.3 deg), the sizable volumetric parameter (= 0.239), and the small difference between the inviscid and viscous L/D values. Observe the relatively small  $\phi_l$  value, which is characteristic of this class of waverider shapes.

Trends for L/D,  $\eta$ , and  $\phi_l$  are shown in Figs. 6-8 in which  $M_{\infty d}=8$ ,  $\delta=10$  deg, and the nonvarying parameters have their nominal value. Large L/D and  $\eta$  values (see Fig. 6) favor  $\Omega_{\infty}$  values around 30-40 deg, and a relatively small  $\phi_l$ . The sharp drop in L/D occurs when  $\Omega_{\infty} \to \Omega_{\infty, \max}$ , in which case  $\eta \to \infty$ ,  $\phi_l \to 0$ , and the waverider degenerates to a vertically oriented plate. While a conventional slender waverider has an  $\eta$ , typically in the range 0.12-0.19, the other slender waverider extreme has  $\eta > 0.3$ . Thus, nonslender waveriders should have an intermediate  $\eta$  value. Observe that once  $\Omega_{\infty}$  is well below  $\Omega_{\infty, \max}$ , both L/D and  $\eta$  are insensitive to it.

Figure 7 shows variations with respect to  $\omega_{\tau}$ . Although the shape of a waverider in the base plane depends on  $\omega_{\tau}$ , as will be discussed, neither L/D or  $\eta$  are sensitive to it. The reason for this is that  $\tau$  is normalized with  $\delta$ , and it is L/D and  $\eta$  that are strongly  $\delta$  dependent. Figure 8 shows a similar plot with  $\omega_{\Lambda}$  as the independent parameter. A value for  $\omega_{\Lambda}$  near 0.7 is favored. The zero values for  $\phi_I$  and L/D when  $\omega_{\Lambda}=0.54$  occur because  $\phi_I$  is  $\omega_{\Lambda}$  dependent, as evident in Eq. (7). Note that  $\phi_I$  does not depend on  $\omega_{\tau}$ ; hence, the relatively flat curves in Fig. 7. Moreover, when  $\phi_I$  is not too small, Figs. 7 and 8 show that  $\omega_{\tau}$  and  $\omega_{\Lambda}$  have little effect on L/D. Thus, for a

Table 1 Properties of HSDT waveriders

Configurations	1	2.	3	4	5	6	7	8	9	10	11	12	13
$\dot{M}_{\times d}$	8	8	8	8	8	8	8	8	8	8	8	8	4
δ	10	6	10	10	10	10	10	10	10	10	10	10	15
$\Omega^{x}$	30	-40.4	0	10	20	0	10	20	30	20	40	30	30
$\omega_{\Lambda}$	1	0	0.5	0.5	0.5	0.5	0.5	0.5	1	1	1	1	1
$\omega_{ au}$	0.7	0.3	0.5	0.5	0.5	0.9	0.9	0.9	0.5	0.7	0.7	0.9	0.7
$\Lambda_b$	24.3	3.63	15.9	15.9	15.9	15.9	15.9	15.9	24.3	24.3	24.3	24.3	18.1
τ	0.888	0.763	0.860	0.851	0.847	0.920	0.914	0.911	0.858	0.898	0.881	0.918	0.883
$\phi_l$	27.2	50.0	28.8	18.8	8.8	28.8	18.8	8.8	27.2	37.2	17.2	27.2	24.0
$b/l_w$	0.344	0.490	0.449	0.325	0.162	0.303	0.209	0.101	0.432	0.428	0.232	0.289	0.509
$S_{\kappa}/S_{\rho}$	2.49	2.08	2.29	2.67	4.24	2.72	3.47	6.19	2.28	2.25	3.18	2.73	2.72
η	0.239	0.136	0.220	0.244	0.308	0.253	0.285	0.362	0.220	0.225	0.271	0.255	0.256
$C_t \times 10$	0.668	0.249	0.657	0.654	0.652	0.678	0.677	0.676	0.657	0.671	0.666	0.678	1.55
$C_{Dinv} \times 10^2$	0.921	0.174	0.902	0.884	0.874	0.940	0.922	0.911	0.902	0.949	0.902	0.939	2.88
$(\widetilde{L/D})_{\mathrm{inv}}$	7.26	14.3	7.28	7.39	7.46	7.21	7.34	7.42	7.28	7.07	7.38	7.22	5.38
$C_c \times 10^3$	0.137	0.136	0.136	0.137	0.140	0.138	0.140	0.141	0.134	0.135	0.139	0.138	0.194
$C_D \times 10^2$	0.955	0.203	0.933	0.921	0.933	0.978	0.970	0.998	0.932	0.979	0.946	0.977	2.93
L/D	7.00	12.3	7.04	7.10	6.98	6.93	6.98	6.77	7.04	6.85	7.04	6.94	5.28

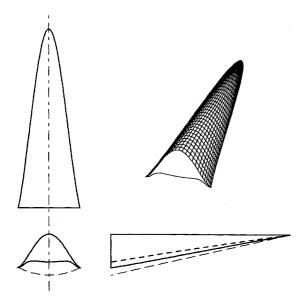


Fig. 5 Scaled views of configuration 1.

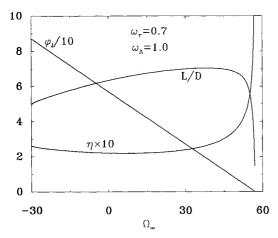


Fig. 6 Variation of  $\phi_l$ , L/D, and  $\eta$  vs  $\Omega_{\infty}$ .

given  $\delta$  value, it is possible to have a large included edge angle and a favorable volumetric distribution without an undue loss in L/D.

Configuration 2 is a typical slender waverider; its base plane shape is shown in Fig. 9. While its L/D is larger than that of configuration 1, its viscous drag increment is also larger. The increase in the drag coefficient caused by the boundary layer is only 3.7% for configuration 1, but is 16.7% for configuration 2. This difference increases rapidly with decreasing Reynolds number. Thus, the difference in viscous L/D between slender and nonslender waveriders narrows for either a reduced vehicle length or a higher flight altitude. In addition, configuration 2 has a small  $\eta$  value and an edge angle  $\Lambda_h$  of only 3.6 deg.

Except for configuration 2, all the cases in Table 1 have  $\tau$  close to 0.9. The importance of  $\tau$  is illustrated in Fig. 9 by comparing configuration 2 to the other cases. (All six views are to scale for the same  $l_w$ .) Although configuration 2 has a large shock layer area fraction  $S_b/(S_b + A_b)$  (=0.619) compared to configuration 1 (and 3–12), its spread-out shock layer is less suitable for a scramjet inlet from a structural viewpoint. The  $\phi_l$  value of 50 deg (configuration 2) is a typical slender waverider value. Figures 6 and 8, however, show that a smaller  $\phi_l$  value provides a maximum L/D as well as a more compact scramjet inlet.

While configurations 1 and 4 differ in  $\Omega_{\infty}$ ,  $\omega_{\Lambda}$ , and  $\omega_{\tau}$ ; the base plane shapes are similar, as are the L/D and  $\eta$  values. The principal difference arises in the value of  $\Lambda_b$ , with con-

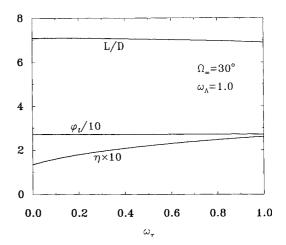


Fig. 7 Variation of  $\phi_l$ , L/D, and  $\eta$  vs  $\omega_{\tau}$ .

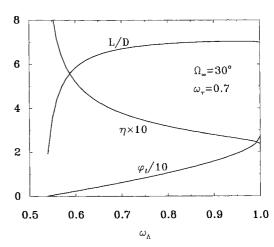


Fig. 8 Variation of  $\phi_l$ , L/D, and  $\eta$  vs  $\omega_{\Lambda}$ .

figuration 4 having a smaller value. Configurations 10-12 in Fig. 9 illustrate the effect of  $\Omega_{\infty}$  and  $\omega_{\tau}$ . Inserts in the figure show enlarged leading-edge views for two configurations. Note the very sharp edge of configuration 2. Even a small amount of rounding would remove a significant portion of the structure, with a large adverse impact on L/D as compared to a less sharp-edged waverider. In its full view, configuration 11 appears to have a sharp-edged winglet, however, the insert shows this not to be the case, since  $\Lambda_b = 24.3$  deg.

The narrow span of configuration 11 is evident from its  $S_w/S_p$  value of 3.18 and  $\phi_l$ , which is only 17.2 deg. Narrow waveriders are characterized by large values for  $\eta$  and  $S_w/S_p$ , and small values for  $\phi_l$  and the aspect ratio  $b/l_w$ . Configurations 5, 7, and 8 are in this category. The L/D of these configurations is less than most of the others because of their larger wetted surface area, and therefore, increased viscous drag.

Configuration 13 is for  $M_{\infty d}=4$  and  $\delta=15$  deg (Table 1 and Fig. 9). Its geometric properties are similar to some of the  $M_{\infty d}=8$  configurations, while its L/D has decreased to 5.28. Its large  $\Lambda_b$  value and base area  $A_b$  stem from the large  $\delta$  value. The other lift and drag parameters for this configuration in Table 1 are larger because of the  $M_{\infty d}^2$  normalization. In this regard,  $C_L$ ,  $C_D$ , and  $C_f$  are normalized with the planform area.

The lower L/D value at  $M_{\sim d}=4$  is typical of both slender and nonslender waveriders. This value would significantly increase if a smaller  $\delta$  value is chosen. However, a smaller value for  $\delta$  results in a sharp reduction in both  $\eta$  and  $\Lambda$ . As a consequence of this tradeoff, it appears that the nonslender

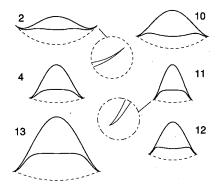


Fig. 9 Base plane views of selected waveriders from Table 1, where numbers denote the configuration.

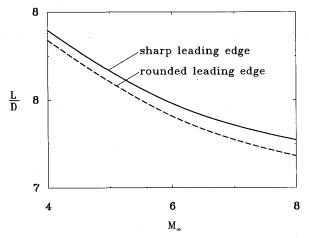


Fig. 10 L/D at off-design Mach numbers for configuration 1 with  $\alpha=0$ , and with sharp and rounded leading edges.

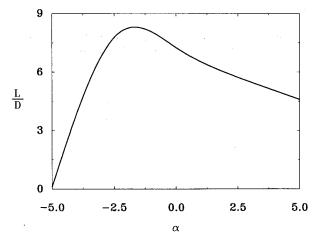


Fig. 11 L/D vs  $\alpha$  for configuration 1 when  $M_{\infty d}=8.3$ .

approach may be most viable for hypersonic design Mach numbers in the medium-to-high range.

## **Off-Design Results**

The CFD calculations are only performed for the configuration 1 nominal case. Even though the shock appears to be attached to the leading edge at  $M_{\infty}=8$ , there remains a small disturbance on the freestream surface near the edge. This is caused by the HSDT shapes, which are only approximate. This disturbance disappears when  $M_{\infty}=8.3$ , and this Mach number is regarded as the on-design value for this waverider shape. The off-design Mach numbers range from 4 to 8.3,

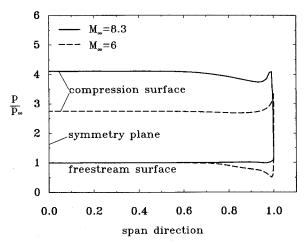


Fig. 12 Pressure distribution in the base plane at  $M_{\infty}=6$  and 8.3 for configuration 1 with sharp leading edge at  $\alpha=0$ .

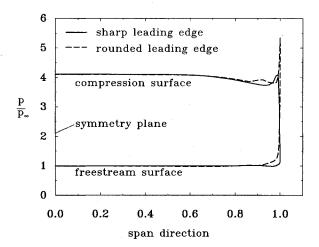


Fig. 13 Pressure distribution in the base plane at  $M_{\infty}=8.3$  for configuration 1 with sharp and rounded leading edges at  $\alpha=0$ .

while the angles of attack, at  $M_{\infty} = 8.3$ , range from -5 to +5 deg.

Figure 10 shows L/D as a function of  $M_{\infty}$  at zero angle of attack. At Mach numbers lower than the on-design value, L/D increases as  $M_{\infty}$  decreases. Figure 11 shows L/D vs  $\alpha$  with a maximum L/D occurring at -1.9 deg. The zero L/D value occurs near -5 deg, which is approximately  $\alpha = -\delta/2$ . Figure 12 shows the pressure distribution in the base plane for  $M_{\infty} = 6$  and 8.3. When  $M_{\infty} < M_{\infty d}$ , a low-pressure region develops on the freestream surface and a high-pressure region is on the compression surface, with both regions near the leading edge. These regions contribute to a higher L/D when  $M_{\infty} < M_{\infty d}$ . The large pressure gradient at the leading edge requires a smaller marching step in the Euler calculations. The L/D trends, however, are similar for slender and non-slender waveriders with aerodynamic properties slightly less sensitive at off-design conditions for a nonslender waverider.

Waverider results with a rounded edge are shown in Figs. 10 and 13. The rounded edge L/D is only a few percent less compared to the L/D for a sharp leading edge. This suggests that rounding has only a local effect, and the nature of the inviscid flowfield around the waverider is unchanged. The pressure distribution in the base plane when  $M_{\infty}=8.3$  shows this limited effect, with a pressure increase only in a small region near the leading edge.

# **Concluding Remarks**

An analytical/computational study is presented of the geometric and aerodynamic properties of waveriders. To enhance

their application, several features are discussed: increase the body's thickness, especially in the base plane, increase the included angle at the leading edge, and uniformly round the leading edge. These changes come at the price of a reduced lift-to-drag ratio. Nevertheless, the L/D is still large, particularly if the waverider is designed for flight at a substantial Mach number. On-design configurations are examined, primarily at  $M_{red} = 8$ , using hypersonic small-disturbance theory. A body-oriented design procedure is developed along with constraints. A Euler code is used to examine off-design performance caused by a reduction in the flight Mach number, angle of attack, and leading-edge rounding. Leading-edge rounding causes a small reduction in L/D, while a variation in the angle of attack results in comparable performance to slender waveriders. When  $M_{\infty} < M_{\infty d}$ , the bow shock stands off from the vehicle's surface, i.e., there is no shock wave boundary-layer interaction, and the L/D is increased from its design value. Thus, there are important benefits to be obtained by designing the waverider at its highest anticipated flight Mach number when in endoatmospheric flight.

# Acknowledgment

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